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# COMPUTER SECURITY

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# Cryptography: THE security mechanism <sup>1</sup>

"Security!" --> "1676c0cf7e901d443bd9cad6c5253fee"

(AES cipher, ECB mode, PKCS#7 padding, 128-b key: "I am JohnDoe 007";  
French quotes are just delimiters.)

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<sup>1</sup> However, keep in mind: «*Cryptography is rarely ever the solution to a security problem.*» (D. Gollmann, Computer Security, p. 203)

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# Basics

## History

- Originally:
  - science (and art) of secret writing
  - aimed at hinder the knowledge of sensitive information
- Currently:
  - science (and art?) of providing mechanisms to ensure security properties (confidentiality, integrity...)
  - aims to control the access to information

## Practical uses

- Traditional:
  - control access to information by **concealing** it, i.e. making it unintelligible
- Modern:
  - the traditional, plus
  - control access to information by **identifying** it with a *fingerprint* (or *hash*<sup>1</sup>)
  - **support** all above uses and
    - produce (almost) random numbers
    - derive secret numbers (keys)<sup>2</sup>

## Relevant types of professionals:

- *cryptographers* - try to master and enhance that access control
- *cryptanalysts* - try to break the enabled access control

1 PT: *síntese, sumário*

2 pieces of data necessary for using cryptographic security mechanisms

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*...Basics...*

**Notation**

<i>Symbol</i>	<i>Name of symbol</i>	<i>Meaning of symbol</i>
<b><i>P</i></b>	plaintext <sup>1</sup>	original, uncovered information
<b><i>E</i></b>	enciphering algorithm	method to conceal the info
<b><i>K<sub>e</sub></i></b>	enciphering key	parameter of the concealment methods
<b><i>C</i></b>	ciphertext	hidden information
<b><i>D</i></b>	deciphering algorithm	method to recover the original info
<b><i>K<sub>d</sub></i></b>	deciphering key	parameter of the recovering methods
<b><i>H, h</i></b>	hash algorithm, hash value	method to transform (hash) the info, transformed info
<b><i>F</i></b>	fingerprint, hash value	transformed info

1 PT: texto inteligível

**...Basics: Notation...**

<b>Operation</b>	<b>Symbolic representation</b>	<b>If...</b>	<b>Cryptography type</b>
cipherring	$C = E_{K_e}(P)$	$K_e = K_d$	symmetric
	$C = E(P, K_e)$ $C = K_e(P)$		
deciphering	$P = D_{K_d}(C)$	$K_e = K^+$ $K_d = K^-$	public-key (asymmetric)
	$P = D(C, K_d)$		
	$P = K_d(C)$		
(cryptographic) hashing <sup>1</sup>	$h = H(P)$ $F = H(P)$ $F = h(P)$		
reversing	$D_{K_d}(E_{K_e}(P)) = P$		

*Advance notice for Digital Signature:*

$$[Doc]_E \iff K_E^-(Doc) \iff K_E^-(H(Doc))$$

<sup>1</sup> Note: *cryptographic* hashing is different from *database* hashing.

## ...Basics...

### Traditional use of Cryptography

- confidentiality protection:
  - conceal information, by making it unintelligible
  - *elsewhere* or *later*, retrieve original information

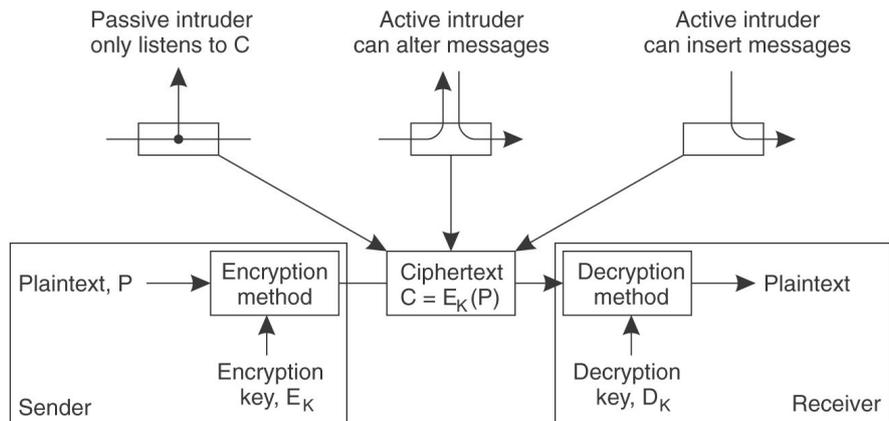


Fig. Original Cryptography: basic model of concealment and recovery of info with examples of attacks (in several of Tanenbaum's books).

## ...Basics...

### Added, newer, usage of Cryptography

- integrity protection:
  - information is *fingerprinted*, by calculating its *hash (or digest)*<sup>1</sup>
  - *elsewhere* or *later*, the hash will be used to detect the adulteration of the original information

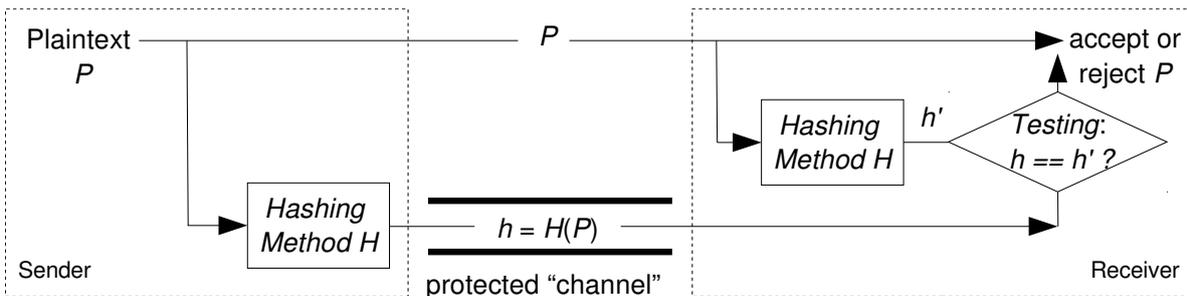


Fig. Newer use of Cryptography: basic model for the validation of info (e.g. integrity protection).  
Note the need for a protected channel!

<sup>1</sup> small array of bytes that represents the original information

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## ...Basics...

### Breaking cryptographic systems

- Professionals: cryptanalysts, random crackers
- Methods: mathematics, statistics, intuition<sup>1</sup>
- Goals: depend on type of usage

### *Attacks in traditional use*

- Goal: grasp the deciphering key! Sometimes, at least, grasp plaintexts.
- Approaches (in descending order of difficulty):
  - normal
    - only ciphertexts are available
  - known original text (“passively” obtained)
    - both some original texts and their enciphered counterparts are available
  - planned original text (“actively” prepared)
    - specific original texts are made to be enciphered

<sup>1</sup> For an example, see Bishop: "Introduction", Chap.8; "Art & Science", chap.9.

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## ***...Basics: Breaking cryptographic systems...***

### ***Attacks in added recent usage***

- Goal: break integrity protection
- Approaches<sup>1</sup> (in descending order of difficulty):
  - find collisions<sup>2</sup>
    - produce document pairs (*birthday attack*<sup>3</sup>)
    - produce another document for a specific original

1 the special case of "digital signatures" will be seen elsewhere

2 meaning: different documents with same fingerprint

3 [https://en.wikipedia.org/wiki/Birthday\\_attack](https://en.wikipedia.org/wiki/Birthday_attack)

## Ideal cryptographic system's requirements

- hard to break
  - in a reasonable future horizon
  - formal proof *would* be nice...<sup>1</sup>
- easy to use
  - otherwise will be rejected or bypassed by users
- if broken, easily replaceable
  - this should be a must, as systems **will** be broken!
  - depends on what was broken (type of secret)

1 Such as Shannon's proof for systems with *perfect secrecy* (e.g. one-time pad):  
<https://web.archive.org/web/20120120001953/http://www.alcatel-lucent.com/bstj/vol28-1949/articles/bstj28-4-656.pdf>

# Classification of cryptographic systems

<i>Perspective</i>	<i>Variant</i>	<i>Sub-variant</i>	<i>Examples</i>
on the secret	secret algorithm	-	RC4, Crypto1 <sup>(1)</sup>
	secret key(s)	single key, shared-key, symmetric	AES
		two-key, public key, asymmetric	RSA
on the method	stream <sup>(2)</sup>	-	RC4, One-time pad
	block	(pure)	AES, RSA, <sup>(3)</sup> SHA-2
		<i>mixed</i>	AES in CBC
on the purpose	confidentiality protection <sup>(4)</sup>	symmetric	AES
		asymmetric <sup>(5)</sup>	RSA
	integrity (& authentication) protection <sup>(6)</sup>	symmetric <sup>(7)</sup>	HMAC w/ SHA-2
		asymmetric <sup>(8)</sup>	RSA
	confidentiality & integrity protection	(several design variants)	AES-GCM
	authentication <sup>(9)</sup>	login	Argon2
remote (challenge-response)		SSH w/ ECDSA	

Notes: next page!

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## **...Classification of cryptographic systems**

### **Notes:**

1 originally, both were secret; now, they are not!

2 PT: *contínuo, sequencial*

3 many authors do not ever classify asymmetric systems (e.g. RSA) as "block"... (more on this later)

4 bidirectional, reversible, two-way operation

5 usually, with "short texts"

6 unidirectional, irreversible, one-way operations

7 using MIC/MAC

8 using digital signatures

9 main usage, with personal and durable (long-lasting) keys

## ...Classification of cryptographic systems

### On the secret

<i>Perspective</i>	<i>Variant</i>	<i>Comments</i>	<i>Exs</i>
on the secret	secret algorithm	<ul style="list-style-type: none"> <li>used in closed applications: military, commercial</li> <li>not recommended by academics<sup>1</sup></li> <li>several design variants</li> </ul>	RC4, Crypto1
	secret key(s)	<ul style="list-style-type: none"> <li>used everywhere: military, commercial, personal applications</li> <li>recommended by academics<sup>2</sup></li> <li>variants (often used in conjunction):</li> </ul>	
		single, shared-key, symmetric: $K_e = K_d = K$	<ul style="list-style-type: none"> <li>heuristic constructions               <ul style="list-style-type: none"> <li>very efficient computation: good for much data</li> </ul> </li> <li>difficult combination and sharing of keys:               <ul style="list-style-type: none"> <li>preferred for closed environments</li> </ul> </li> </ul>
	two-key, public key, asymmetric: $K_e = K^+ \neq K_d = K^-$	<ul style="list-style-type: none"> <li>math-based constructions               <ul style="list-style-type: none"> <li>very heavy computation: only for little data</li> </ul> </li> <li>easy combination and exchange of keys:               <ul style="list-style-type: none"> <li>ideal for open environments</li> </ul> </li> </ul>	RSA

1 because, sooner or later, the secret will be discovered and a replacement is always difficult to produce

2 and by common sense as well, if history is something to go by...

## On the method

### “Long” texts <sup>1</sup>

- cryptographic operations<sup>2</sup> have to be done on (equal sized) pieces (blocks) <sup>3</sup>
  - typical size: 8 B (64 b) and 16 B (128 b) <sup>4</sup>
- enciphering (and deciphering)
  - *modes of operation*<sup>5</sup> are ways to use keys in the processing of each piece
- hashing
  - does not use keys (in general)
- final piece might need to be “padded” <sup>6</sup>
  - as, in general, data size is not a multiple of the piece size

1 in practice, almost any text is “long”...

2 ciphering, deciphering, hashing

3  $P = P_1 P_2 \dots$

4 but could be 1 b, 1 B, ...

5 to be discussed later

6 to be discussed later

**...Classification of cryptographic systems: on the method**

<b>Perspective</b>	<b>Variant</b>	<b>Sub-variant</b>	<b>Comments</b>	<b>Exs</b>
on the method	stream		<ul style="list-style-type: none"> <li>• each piece is (de)ciphered with a different key, <math>K = K_1 K_2 \dots</math></li> <li>• e.g. <math>C = K(P) = K_1(P_1) K_2(P_2) \dots</math></li> </ul>	RC4, One-time pad
	block	(pure)	<ul style="list-style-type: none"> <li>• each piece is (de)ciphered with the same key, <math>K</math></li> <li>• e.g. <math>C = K(P) = K(P_1) K(P_2) \dots</math></li> <li>• fingerprinting does not use keys</li> <li>• in general, <math>F = H(P) = H(P_1) H(P_2) \dots</math></li> </ul>	AES, RSA <sup>1</sup> in ECB <sup>2</sup> ;  SHA-2, SHA-3 <sup>3</sup>
		<i>mixed</i>	<ul style="list-style-type: none"> <li>• each piece is (de)ciphered with a "virtual" different key, based on the same key</li> </ul>	AES in CBC <sup>4</sup>

- 1 Many authors do not consider RSA to be a block cipher, as it is not efficient enough to be used consecutively (block after block) in long documents. E.g., see section 3.5 of Peter Gutmann, [Lessons Learned in Implementing and Deploying Crypto Software](#).
- 2 Electronic Code Book
- 3 SHA: Secure Hash Algorithms
- 4 Cipher Block Chaining

*...Classification of cryptographic systems*

## On the purpose

<i>Perspective</i>	<i>Variant</i>	<i>Sub-variant</i>	<i>Examples</i>	<i>Usage ex.</i>
on the purpose	confidentiality protection <sup>1</sup>	symmetric <sup>2</sup>	AES	Fig. Cs below
		asymmetric <sup>3</sup>	RSA	Fig. Ca below
	integrity (& authentic.) protection <sup>4</sup>	symmetric <sup>5</sup>	HMAC w/ SHA-2	Fig. Is below
		asymmetric <sup>6</sup>	RSA	Fig. Ia below
	confidentiality & integrity protection	(several design variants)	AES-GCM	Fig. CI below
	authentication <sup>7</sup>	login	Argon2	Fig. A1 below
remote (challenge-response)		SSH w/ ECDSA	Fig. A2 below	

- 1 bidirectional, reversible, two-way operation
- 2 usually, with ephemeral keys
- 3 usually, with "short texts"
- 4 unidirectional, irreversible, one-way operation
- 5 using MIC/MAC
- 6 using digital signatures
- 7 main usage, with personal and durable (long-lasting) secrets

**...Classification of cryptographic systems: on the purpose...**

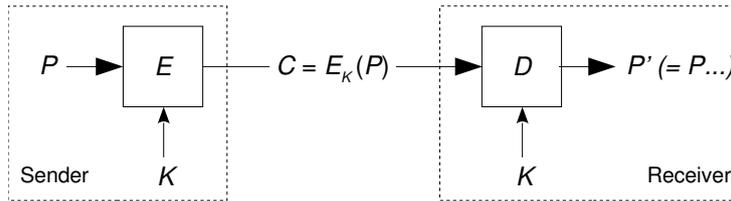


Fig Cs. Confidentiality with symmetric cryptography.

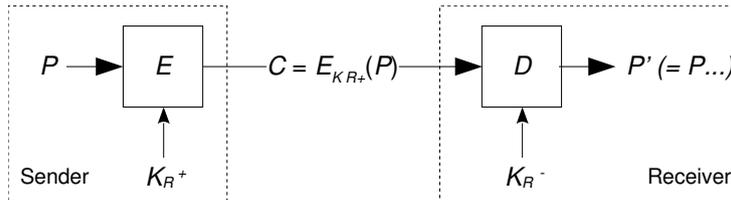


Fig Ca. Confidentiality with asymmetric cryptography.

**...Classification of cryptographic systems: on the purpose...**

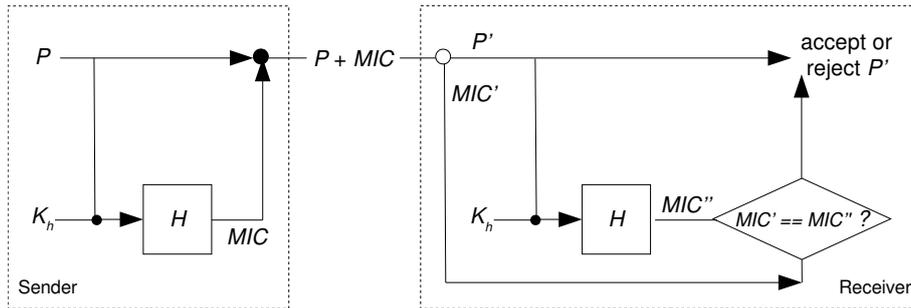


Fig 1s. Integrity (& Authentication) with Message Integrity/Authentication Code.

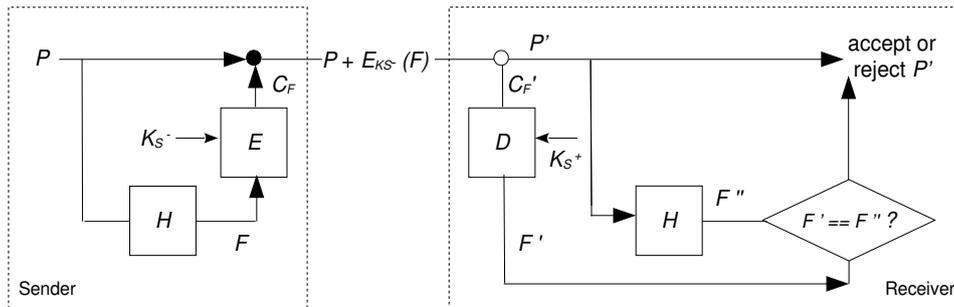


Fig 1a. Integrity (& Authentication) with Public-key Digital Signature.

...Classification of cryptographic systems: on the purpose

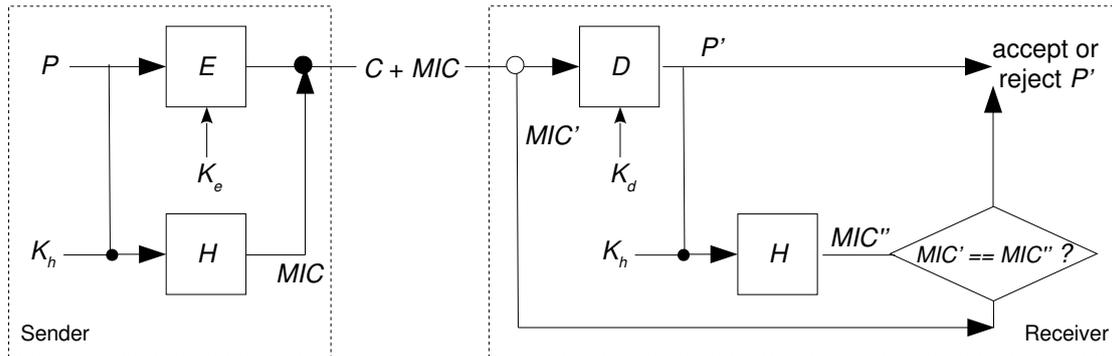


Fig CI. Confidentiality & Integrity (Authenticated Encipherment).

...Classification of cryptographic systems: on the purpose

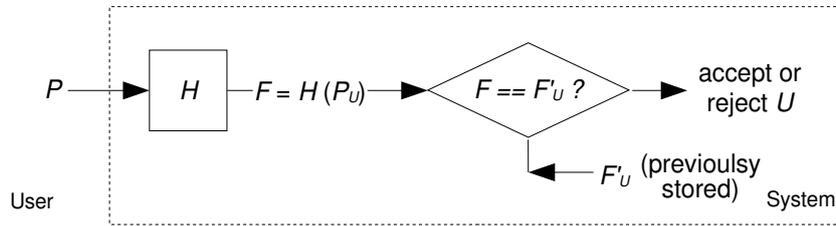


Fig A1. Authentication with cryptographic hashing.

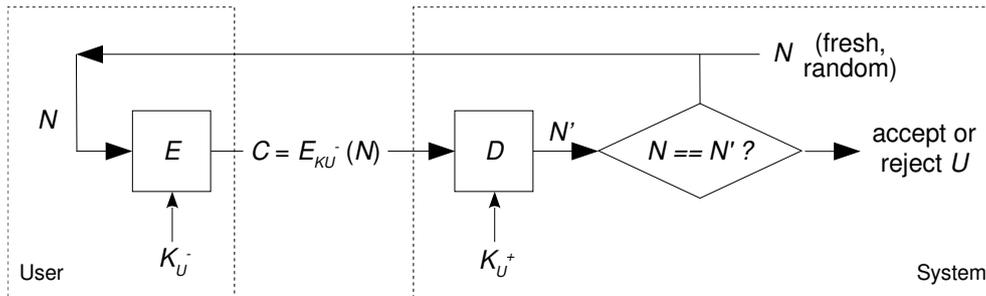


Fig A2. Authentication with asymmetric cryptography.

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# Cryptographic Keys

## Definition

- cryptographic key – piece of data needed for cryptographic operations
  - usually: number or string hard to memorize
  - some times: fit to a mathematical procedure (algorithm)<sup>1</sup>
  - most of the times: secret

## Key types of cryptographic keys

<i>Designation</i>	<i>"Owner" entity</i>	<i>Main application</i>	<i>Cryptographic type</i>	<i>Longevity</i>	<i>Efficiency</i>
personal	human	authentication	public-key	extended	low
session	communication channel	confidentiality	shared-key	short <sup>2</sup>	high <sup>3</sup>

- 1 so, user cannot "choose" it: a "cryptographic key generator" is needed
- 2 to be usage-resistant (prevent brute-force search and repetition attacks)
- 3 so, can accommodate heavy traffic

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## Key Management

- generation
  - problem solved: just take care with choosing of seed values<sup>1</sup>
- storage
  - many "solutions", but still a problem swept under the rug!
- distribution
  - big problem:
    - physically separated entities must exchange/agree on cryptographic keys
  - solutions:
    - several, depending on type of cryptography
      - symmetric: e.g. Diffie-Hellman key exchange
      - asymmetric: e.g. digital certificates carry public key

<sup>1</sup> here, randomness is essential

## ...Key Management: Digital Certificate...

### Digital certificate

- document that maps an entity to a cryptographic public key
  - the mapping is guaranteed by  $T$ ,<sup>1</sup> by digital signing the document<sup>2</sup>

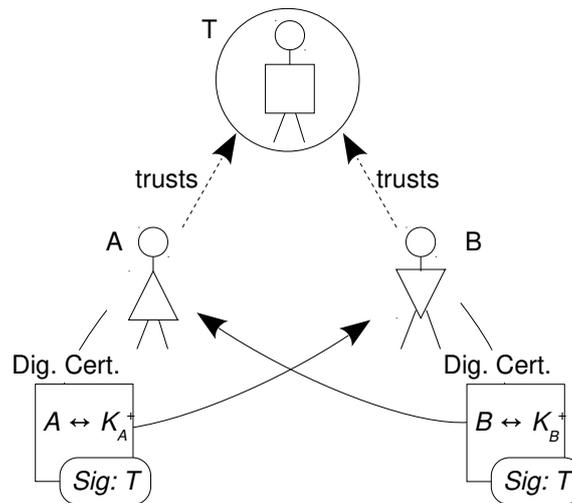


Fig. Representation of users, trusted certificate emitter and digital certificate's essential content.

- 1  $T$  is entity trusted by  $A$  and  $B$ : 1- they believe  $T$  operates in an honest way; 2- they have previously exchanged cryptographic info with  $T$ . Usually, but not necessarily,  $T$  is connoted with a *Certification Authority* (CA).
- 2 so, assuring the legitimacy of the certificate's content; technique will be discussed later

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## ...Key Management: Digital Certificate

### Typical content

I hereby certify that the public key 19836A8B03030CF83737E3837837FC3s87092827262643FFA82710382828282A belongs to Robert John Smith 12345 University Avenue Berkeley, CA 94702 Birthday: July 4, 1958 Email: bob@superdupernet.com
SHA-1 hash of the above certificate signed with the CA's private key

Fig. *Really* relevant content type of a digital certificate (*in* several of Tanenbaum's books).

- identity of key's owner
- his/her public key
- identity of emitter<sup>1</sup>
- digital signature of emitter
- expiration date of certificate
- serial number
- specific purpose
- etc.

1 e.g. typically, a Certificate Authority

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# Randomness

- essential in Cryptography!
  - one time pad, IV (initialization values), stream cipher seeds
  - hashes
  - *nonces*, key generation (e.g. asymmetric keys)...
- generation
  - excellent: physical source
    - inherent: radioactive decay, Brownian movement, ...
    - depending on initial conditions: (non-biased) roulette, dice, ...
  - reasonable: algorithmic-based with physical seed
    - cryptographically secure pseudorandom number generators
      - use physical (hopefully random) sources (e.g. mouse movements)
      - Linux's `getrandom()` (`/dev/random`, `/dev/urandom`)
  - bad: algorithmic-based
    - pseudorandom number generators
      - POSIX's `random()`

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# Cryptographic libraries

- essential in cryptographic programming
  - encryption, hashing, signing... different algorithms... all ready to be used
    - coupled with a "*cryptographically secure pseudorandom number generator*"
  - why not write your own library?
    - Highly dangerous! It is not just implementing algorithms, it is how they are used, how "random" numbers are generated and chosen, etc.<sup>1</sup>
- examples
  - OpenSSL: the reference!<sup>2</sup>
    - components: application & C library
    - EVP (envelope) "high level" API (lab classes)
  - WebCrypto: JavaScript (by W3C)
  - Bouncy Castle: Java and C# (by Australia's Legion...)
  - Libgcrypt: C (OpenPGP library) (by GnuPG community)
  - PyCryptodome: Python

1 see, for instance, <https://security.stackexchange.com/questions/18197/why-shouldnt-we-roll-our-own>

2 in spite of same infamous bugs, such as *The Heartbleed Bug* ([heartbleed.com](http://heartbleed.com))

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# Cryptographic algorithms

- [RC4](#): stream key generation (1987, survives with medication)
- [DES](#)<sup>1</sup>: reversible system, secret key (1975, defunct)
- [AES](#): reversible system, secret key (1998, still healthy)
- [RSA](#)<sup>2</sup>: reversible system, public key (1977, still healthy)
- [MD5](#)<sup>3</sup>: irreversible system (1992, defunct)
- [SHA-1](#)<sup>4</sup>: irreversible system (1995, defunct)
- [SHA-2](#): irreversible system (2001, still healthy)
- [SHA-3](#)<sup>5</sup>: irreversible system (2015, yet in phase of wide adoption)

1 Data Encryption Standard, a landmark of cryptography

2 another landmark of (public-key) cryptography

3 yet another landmark of cryptography

4 about SHA-1 end of life, see [sha-mbles.github.io](https://github.com/sha-mbles)

5 based on new paradigm - sponge construction ([keccak.team/sponge\\_duplex.html](https://keccak.team/sponge_duplex.html))

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# Cryptographic transformations

- diverse, generally follow some major "patterns" for each type of cryptography
- in general, Shannon's recommended properties<sup>1</sup> are followed:
  - *diffusion* – each plaintext unit (e.g. char) affects many transformed units
  - *confusion* – transformed output depends complexly on key (if it exists)

## Common patterns<sup>2</sup> - symmetric cryptography

- Transposition – exchange (swapping) of positions of elements – *P-box*
- Substitution – exchange of elements (e.g. Caesar's cipher) – *S-box*
- Combination - transposition and substitution cascade – *product cipher* [Fig.C]
- Feistel construct (e.g. 3DES) [Fig.F]
- ...

1 Those were thought to symmetric cryptography, the only that existed at the time (1949); however, they are applied, at least partially, to other, contemporary cryptographic systems.

2 or transformations

...Cryptographic transformations: common patterns...

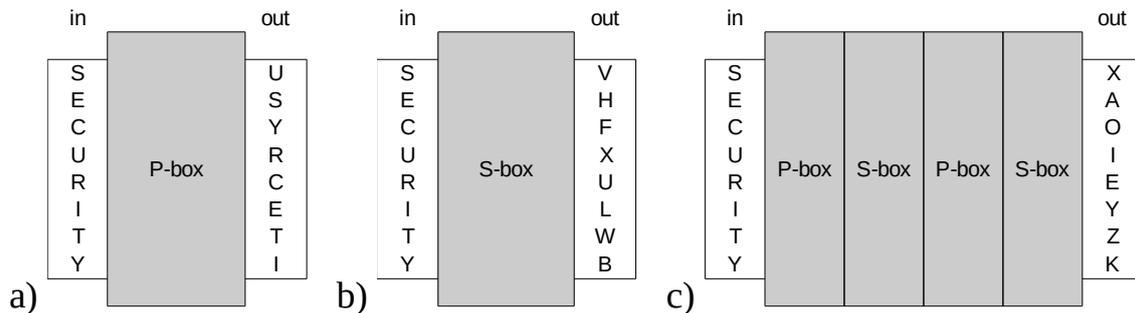


Fig C. Symmetric transformations: a) permutation box; b) substitution box; c) “complete”, product cipher. Exercise: find out the algorithms for P- and S- boxes and validate them with c).

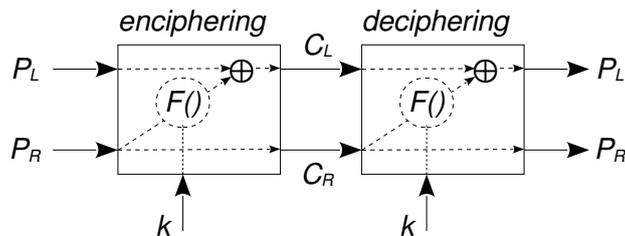


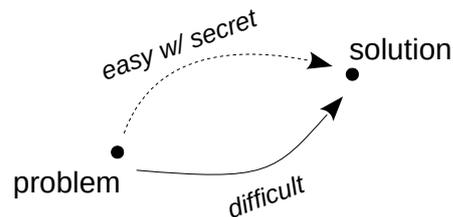
Fig F. Feistel symmetric construct "in action".  $F$  is Feistel (or round) function.

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## ...Cryptographic transformations: common patterns...

### Common patterns - asymmetric constructs

- based on apparent intractability of computational problems:
  - easy to compute with knowledge of some data; otherwise, most difficult (intractable) to compute<sup>1</sup>
  - common computational problems:
    - integer factorization (e.g. RSA)
    - discrete logarithm problem (e.g. DSA)
    - ...



### Common patterns - "hash" cryptography

- most common are *iterated hash functions*
  - Merkle-Damgård construct (e.g. SHA-2)
  - sponge construct (e.g. SHA-3)
  - ...

<sup>1</sup> Informally, an easy or tractable problem can be solved in less than  $n^k$  (polynomial) time units,  $k$  being an integer and  $n$  the size of the problem (e.g. number of items to sort); a hard or intractable problem will need  $k^n$  (exponential) time units to be solved.

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## Some numbers...

- $2^8 = 256$  number of values represented by a byte
- $2^{32} = 4\,294\,967\,296$  maximum number of IPv4 addresses  
 $\approx 0,5 * \text{number of people on Earth in 2023}$
- $2^{56} = 72\,057\,594\,037\,927\,936$  number of different keys for DES algorithm
- $2^{64} = 18\,446\,744\,073\,709\,551\,616$  1+ number of grains of wheat in chess board (from 1, doubled in each square)
- $2^{76} \approx 10^{23}$  mass of the Moon in kg
- $2^{79} \approx 10^{24}$  Avogadro's constant
- $2^{82} \approx 10^{25}$  mass of the Earth in kg
- $2^{101} \approx 10^{30}$  mass of the Sun in kg
- $2^{128} = 340\,282\,366\,920\,938\,463\,463\,374\,607\,431\,768\,211\,456$   
 $\approx 10^{38}$  maximum number of IPv6 addresses
- $2^{256} \approx 10^{77}$  number of values of SHA-256 hash
- $2^{280} \approx 10^{84}$  number of fundamental particles in the observable universe

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## Pointers...

- The “**Public-key cryptography paper**”, 1976 – W. Diffie , M. E. Hellman
  - [www-ee.stanford.edu/~hellman/publications/24.pdf](http://www-ee.stanford.edu/~hellman/publications/24.pdf)
- The “**RSA paper**”, 1978 – R. L. Rivest, A. Shamir, and L. Adleman
  - [dx.doi.org/10.1145/359340.359342](https://dx.doi.org/10.1145/359340.359342)
- The “**ElGamal Signature Scheme**”, 1985 – Taher Elgamal
  - [ieeexplore.ieee.org/stamp/stamp.jsp?arnumber=01057074](http://ieeexplore.ieee.org/stamp/stamp.jsp?arnumber=01057074)
- The “**DES Cryptanalysis paper**”, 1977 – W. Diffie , M. E. Hellman
  - [www-ee.stanford.edu/~hellman/publications/27.pdf](http://www-ee.stanford.edu/~hellman/publications/27.pdf)
- The “**Rijndael, AES Proposal**”, 1999 – Joan Daemen, Vincent Rijmen
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